

Variation - Day 1  
Notes

Name \_\_\_\_\_  
Date \_\_\_\_\_ Period \_\_\_\_\_

Definition: If  $y$  varies directly with  $x$ , then as the value of  $x$  increases, the value of  $y$  also increases.

Equation:  $y = kx$ , where  $k$  is the constant of variation. ( $k$  cannot be 0.)

$k$  can be found by the following equation,  $k = \frac{y}{x}$ .

Example 1

Julio's wages vary directly with the number of hours that he works. If his wages for 5 hours are \$29.75, how much will they be for 30 hours? Let  $x$  = the number of hours he works, and let  $y$  = Julio's pay.

- a. Find the value of  $k$ .  $k =$  \_\_\_\_\_
- b. Write an equation \_\_\_\_\_
- c. Find Julio's pay for 30 hours. Pay \_\_\_\_\_

- Sometimes it is easier to solve a variation by using a proportion and cross multiplying.

Example 2

If  $y$  varies directly with  $x$ , and  $y = 28$  when  $x = 7$ , find  $x$  when  $y = 52$ .

$x =$  \_\_\_\_\_

Practice

1. A standard shower head uses 18 gallons of water in 3 minutes. Complete the table below that shows that gallons used,  $y$ , is a function of time in the shower,  $x$ .

a.

$x$ (minutes)	3	6	9	12	15	20	25	30
$y$ (gallons)								

- b. What is the  $k$ ?  $k =$  \_\_\_\_\_
- c. Write the equation for the function \_\_\_\_\_
- d. If 270 gallons were used, how many minutes were spent in the shower? \_\_\_\_\_

For the following word problems, write an equation and answer each question.

2. Cynthia charges \$4 an hour to walk a dog. How much would she charge for  $2\frac{1}{2}$  hours?

k = \_\_\_\_\_ Equation \_\_\_\_\_ Answer \_\_\_\_\_

3. It takes Maxine  $2\frac{1}{2}$  hours to bake a cake. How long would it take her to bake 4 cakes?

k = \_\_\_\_\_ Equation \_\_\_\_\_ Answer \_\_\_\_\_

4. Damian can type 45 words per minute. How many can he type in 3 hours?

k = \_\_\_\_\_ Equation \_\_\_\_\_ Answer \_\_\_\_\_

5. It takes  $\frac{2}{3}$  of an hour for Chad to wash and wax a car. How long will it take for 7 cars?

k = \_\_\_\_\_ Equation \_\_\_\_\_ Answer \_\_\_\_\_

Solve using proportions. Assume that y varies directly with x.

6. If  $y = 27$ , when  $x = 6$ , find x when  $y = 45$ .  $x =$  \_\_\_\_\_

7. If  $y = 2.5$ , when  $x = 0.5$ , find y when  $x = 20$ .  $y =$  \_\_\_\_\_

8. If  $y = 4$ , when  $x = 12$ , find y when  $x = -24$ .  $y =$  \_\_\_\_\_

9. If  $y = 80$ , when  $x = 32$ , find x when  $y = 100$ .  $x =$  \_\_\_\_\_

10. If  $y = -6$ , when  $x = 9$ , find y when  $x = 6$ .  $y =$  \_\_\_\_\_