

Name _____

Date _____

Reporting Category 5 Notes (A.10.A)

To solve a quadratic equation means to find the roots.

***Remember roots are the same thing as x-intercepts, zeros, or solutions!**

Ultimately, you have to factor the quadratic expression to find the solutions.

Factoring quadratics that are in standard form ($Ax^2 + Bx + C = 0$) can be broken up into specific steps.

Step 1: Make a product/sum table

Example:
 $2x^2 - 11x + 5$

<u>P= 1st term X 3rd term</u>	<u>S= 2nd term</u>
<u>P= 10</u>	<u>S= -11</u>
5, 2	7
-5, -2	-7
10, 1	11
-10, -1	-11

Step 2: Put selected factors in the sets. $(x - 10)(x - 1)$

Step 3: Put each factor over the 1st coefficient. Simplify and reduce.

$$\left(x - \frac{10}{2}\right)\left(x - \frac{1}{2}\right) = \left(x - 5\right)\left(x - \frac{1}{2}\right)$$

Step 4: If the number reduces evenly you're done. If not, take the denominator of the fraction that doesn't become a whole number and swing it up to become the x coefficient. Factors: $(x - 5)(2x - 1)$

Name _____

Date _____

Reporting Category 5 Notes (A.10.A)

Sometimes quadratics don't factor perfectly into whole numbers. When this happens, you must use the Quadratic Formula to solve for the roots.

Quadratics Formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Example: Find the solutions for "x" in the equation $3x^2 = 2x + 1$.

- First, put the equation in standard form.

$$3x^2 - 2x - 1 = 0$$

- Second, state the values of a, b, and c.

$$a = 3, b = -2, c = -1$$

- Then, substitute the values of a, b, and c into the formula:

$$x = \frac{-(-2) \pm \sqrt{(-2)^2 - 4(3)(-1)}}{2(3)}$$

and simplify.....

$$x = \frac{2 \pm \sqrt{4 - (-12)}}{6}$$

$$x = \frac{2 \pm \sqrt{16}}{6}$$

$$x = \frac{2 \pm 4}{6}$$

$$x = \frac{2 + 4}{6} = \frac{6}{6} = 1$$

$$x = \frac{2 - 4}{6} = \frac{-2}{6} = -\frac{1}{3}$$

The solutions to this quadratic equation are (1, 0) and (-1/3, 0)